

Divide:

$$\frac{8(-4+4i)}{(-4-4i)(-4+4i)}$$

$$\frac{-32+32i}{16-16i+16i-16i^2}$$

$$\frac{-32+32i}{16+16}$$

$$\frac{-32+32i}{32}$$

$$-1+i$$

$$\boxed{-1+i}$$

Factor:

$$x^8 - 17x^4 + 16 = 0$$

$$(x^4 - 16)(x^4 - 1) = 0$$

$$(x^2+4)(x^2-4)(x^2+1)(x^2-1)$$

$$(x^2+4)(x+2)(x-2)(x^2+1)(x+i)(x-i)$$

Warm-Up

○ Simplify:

○ $x^{-2}y^4$

○ $\frac{y^3z^{-1}}{z^1}$

○ $\frac{-2x^{-3}x^{-4}}{y^{-8}}$

○ True or false:

- Any number (or variable) to the zero power is 1

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Graphing
Exponentials
and
Exponential
equations

Exponential Functions

- A function $f(x) = ab^x$, $a \neq 0$, with $b > 0$, and $b \neq 1$. The base b is a constant. The exponent x is the independent variable with domain all real numbers.

$$f(x) = ab^x$$

Exponential Functions

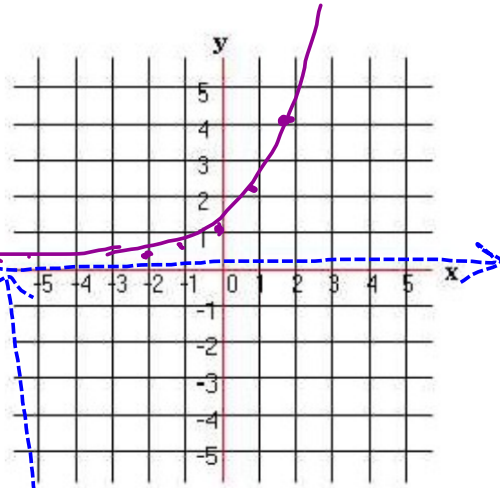
$$y = 2^x$$

x	y
-2	$\frac{1}{4}$
-1	$\frac{1}{2}$
0	1
1	2
2	4

$$2^{-2} = \frac{1}{2^2} = \frac{1}{4}$$

$$2^{-1} = \frac{1}{2^1} = \frac{1}{2}$$

$$2^{-5} = \frac{1}{2^5} = \frac{1}{32}$$



HA $y = 0$

y-int : 1

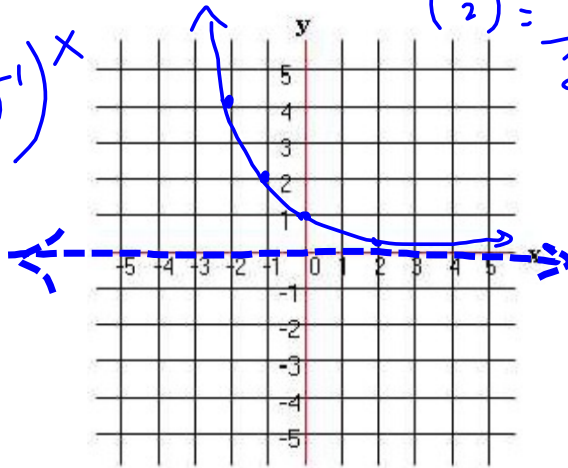
horizontal
Asymptote

(line that the graph approaches but never touches)

Exponential Functions

Decay
 $y = \left(\frac{1}{2}\right)^x = (2^{-1})^x$
 $= 2^{-x}$

HA $y = 0$
 y-int = 1



$\left(\frac{1}{2}\right)^2 = \frac{1}{2^2} = \frac{1}{4}$
 $\left(\frac{1}{2}\right)^{-1} = \frac{1}{2^{-1}} = 2^1 = 2$

Exponential Functions

For the function $y = ab^x$

--if $a > 0$ and $b > 1$, the function represents exponential growth.

--if $a > 0$ and $0 < b < 1$, the function represents exponential decay.

In either case, the y-intercept is $(0,a)$, the domain is all real numbers, the asymptote is $y = 0$, and the range is $y > 0$.

Exponential Functions

$$y = e^x$$

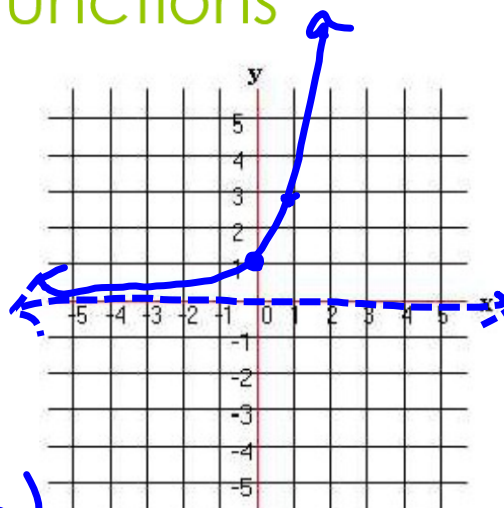
$$(2.718)^x$$

$$HA \ y = 0$$

$$y\text{-int} = 1$$

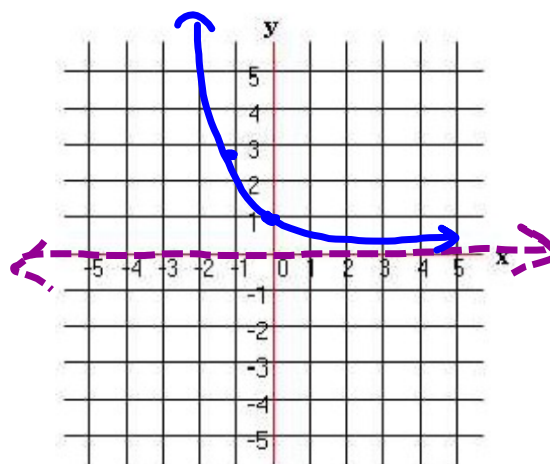
$$\text{Domain } (-\infty, \infty)$$

$$\text{Range } (0, \infty)$$



Exponential Functions

$$y = \left(\frac{1}{e}\right)^x$$



Exponential Functions- Transformations

- $y = f(x)$ 2^x Parent Function 2^x
- $y = f(x) \pm a$ up or down translation $2^x + 4$
- $y = f(x \pm a)$ left or right translation 2^{x+3}
- $y = -f(x)$ reflection across x-axis -2^x
- $y = f(-x)$ reflection across y-axis 2^{-x}
- $y = af(x); a > 1$ pull toward y-axis $3(2^x)$
- $y = af(x); 0 < a < 1$ pull toward x-axis $\frac{1}{2}(2^x)$

Transformations

$$y = 2^{x-3}$$

↑
Right 3

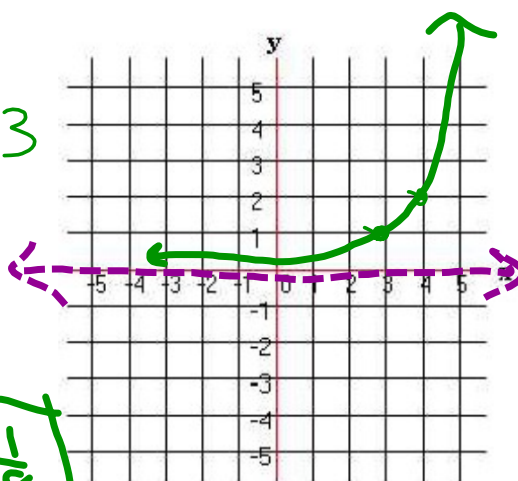
HA $y = 0$

y-int

$$2^{0-3} = 2^{-3} = \frac{1}{2^3} = \frac{1}{8}$$

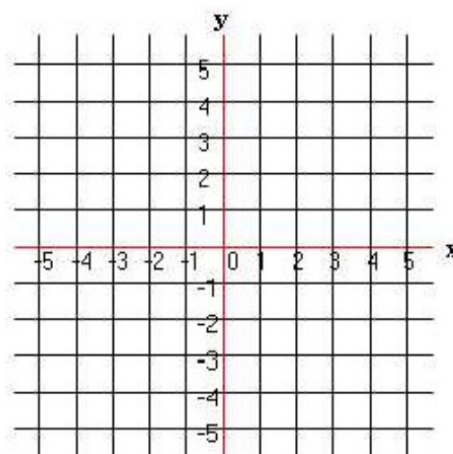
D: $(-\infty, \infty)$

R: $(0, \infty)$



Transformations

$$y = \left(\frac{1}{2}\right)^{x+2}$$



Transformations

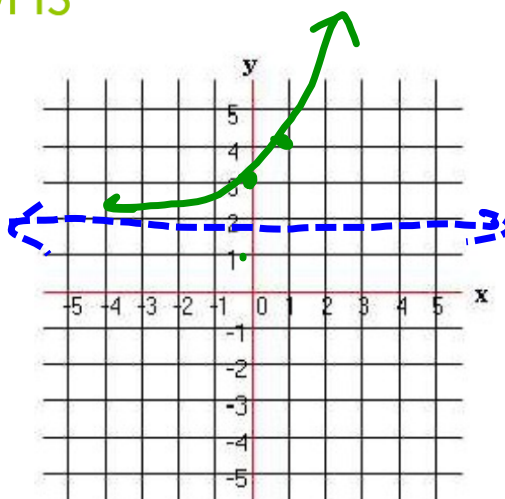
$$y = 2^x + 2$$

↑
up

HA $y = 2$

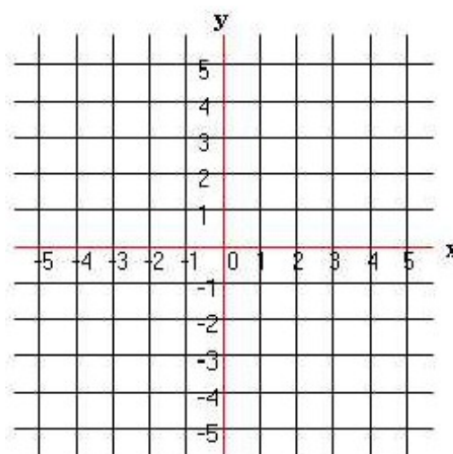
D: $(-\infty, \infty)$

R: $(2, \infty)$



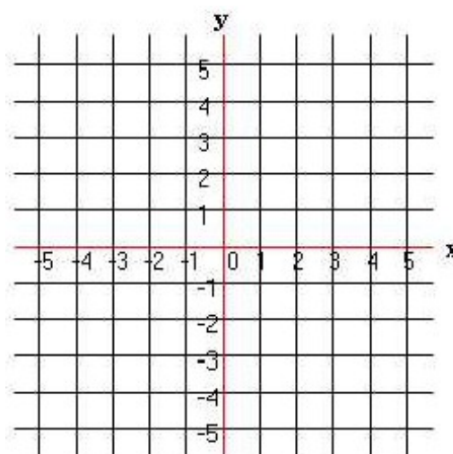
Transformations

$$y = \left(\frac{1}{2}\right)^x - 3$$



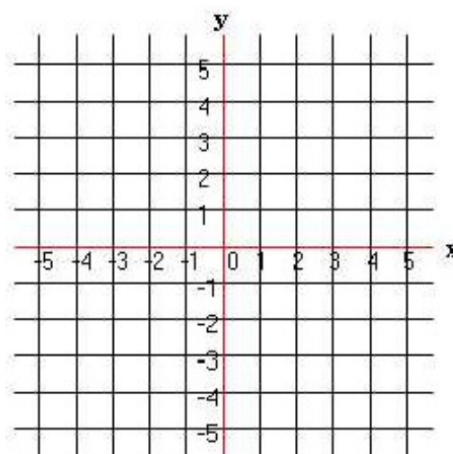
Transformations

$$y = 2(2^x)$$



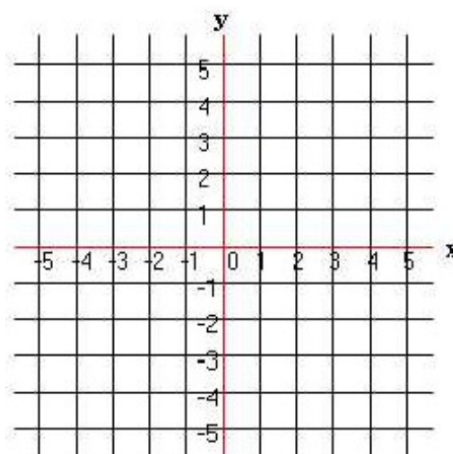
Transformations

$$y = 3 \left(\frac{1}{2} \right)^x$$



Transformations

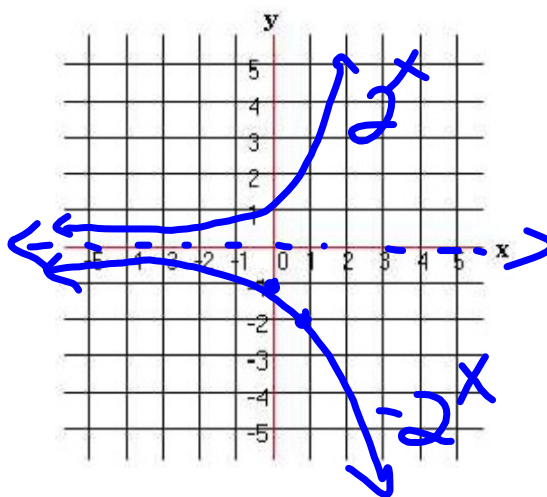
$$y = \frac{3}{4}(2)^x$$



Transformations

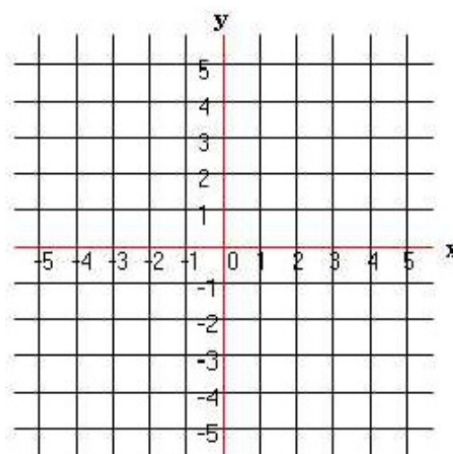
$$y = -2^x$$

$$-2^0$$
$$-2^1$$



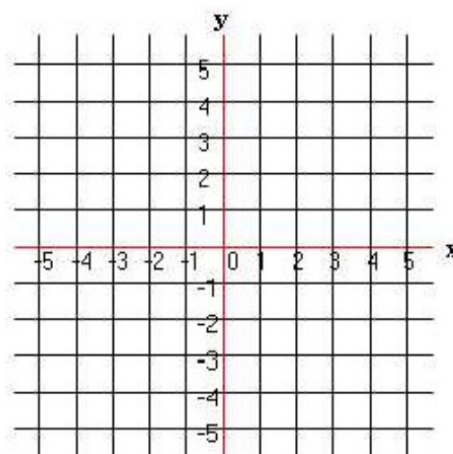
Transformations

$$y = -3 \left(\frac{1}{2} \right)^x$$



Transformations

$$y = 3^{x-2} + 3$$



Transformations

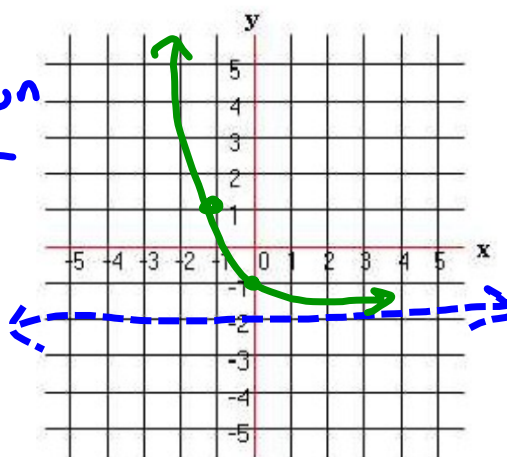
$$y = (3^{-x}) - 2$$

↑
reflects
over y

↑
down
2

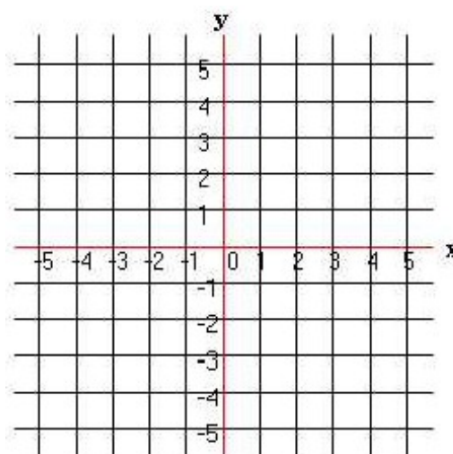
HA $y = -2$

$$3^{-(-1)} - 2$$



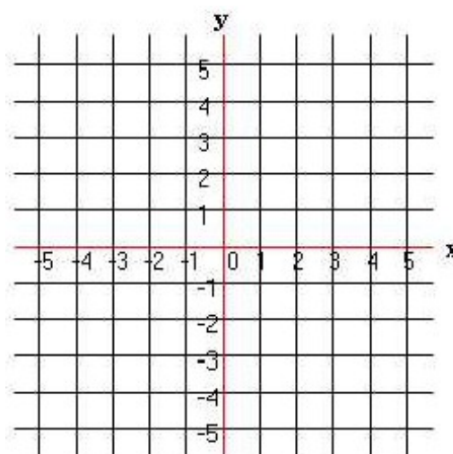
Transformations

$$y = -4(3^{x-1}) + 1$$



Transformations

$$y = -\left(\frac{1}{5}\right)^{x+2} - 2$$



Solving Exponential Equations

Exponential Equation—equation with the variable in the exponent

Steps to follow:

1. Match bases if possible
2. Drop bases and simplify using exponent laws.
3. Solve for the variable.

Solving Exponential Equations

$$2^x = 2^4$$

$$x = 4$$

① Make the bases the same

② If the bases are the same, the exponents are equal.

Set the exponents equal to each other & solve.

Solving Exponential Equations

$$2^x = 2^{3x-1}$$

$$x = 3x - 1$$

$$-3x$$

$$-2x = -1$$

$$x = -\frac{1}{2}$$

Solving Exponential Equations

$$5^{3x} = 25^{x+2}$$

$$5^{3x} = (5^2)^{x+2}$$

$$5^{3x} = 5^{2x+4}$$

$$3x = 2x + 4$$

$$-2x$$

$$x = 4$$

Solving Exponential Equations

$$4^{2x-5} = 16^{3x}$$

Solving Exponential Equations

$$25^{x-4} = 125^{4x+3}$$

$$(5^2)^{x-4} = (5^3)^{4x+3}$$

$$5^{2x-8} = 5^{12x+9}$$

$$2x - 8 = 12x + 9$$

$$-8 = 10x + 9$$

$$-17 = 10x$$

$$\boxed{-\frac{17}{10} = x}$$

Solving Exponential Equations

$$2^{x-1} = \left(\frac{1}{8}\right)^{x+3}$$

$$2^{x-1} = \left(\frac{1}{2^3}\right)^{x+3}$$

$$2^{x-1} = (2^{-3})^{x+3}$$

$$2$$

$$2^{-3}$$

$$x-1 = -3x-9$$

$$+3x$$

$$4x-1 = -9$$

$$+1$$

$$4x = -8$$

$$\boxed{x = -2}$$

Solving Exponential Equations

$$\left(\frac{1}{64}\right)^{x^2} = \left(\frac{1}{16}\right)^8$$

Solving Exponential Equations

$$4^x \cdot \left(\frac{1}{64}\right)^{5x-3} = \left(\frac{1}{16}\right)^{x-6}$$

$$4^x \cdot (4^{-3})^{5x-3} = (4^{-2})^{x-6}$$

$$4^x \cdot (4)^{-15x+9} = 4^{-2x+12}$$

$$4^{x-15x+9}$$

$$4^{-14x+9} = 4^{-2x+12}$$

$$-14x + 9 = -2x + 12$$

$$+14x$$

$$9 = 12x + 12$$

$$-12$$

$$-3 = 12x$$

$$\boxed{-\frac{3}{12} = x}$$

$$\boxed{-\frac{1}{4} = x}$$

Solve:

$$(0.25)^{7x} = 32^{x-7}$$

$$\left(\frac{1}{4}\right)^{7x} = 32^{x-7}$$

$$(2^{-2})^{7x} = (2^5)^{x-7}$$



